## CA2803 STATISTICAL METHODS FOR COMPUTER APPLICATIONS Set 2

Note : Statistical Tables will be provided.

## PART A

## Answer ALL Questions

( $10 \times 2=20$ )

1. What is standard deviation?
2. Define correlation
3. What is mathematical expectation?
4. Probability lies between $\qquad$ and $\qquad$
5. Define Poisson distribution
6. State true or false the following:

For a binomial distribution, mean is 24 and variance is 12 .
7. Define the terms: i. Parameter ii. Statistic
8. What are null hypothesis and alternative hypothesis.
9. What is moving average?
10. What methods are used to find cyclic variations?

## PART B

## Answer ALL Questions

( $5 \times 8=40$ )
11a. Runs scored by two batsmen, batsman A and batsman B in an innings of 10 matches is given below. Who is more efficient and who is more consistent?

| Batsman A | 10 | 115 | 5 | 73 | 7 | 120 | 36 | 84 | 29 | 19 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Batsman B | 45 | 12 | 76 | 42 | 4 | 50 | 37 | 48 | 13 | 0 |

11b. In order to find the correlation coefficient between two attributes $X$ and $Y$ from 20 pairs of observations, the following calculations were made: $\sum \mathrm{X}=120, \sum \mathrm{Y}=80, \sum \mathrm{X}^{2}=1440, \sum \mathrm{Y}^{2}=$ $650, \sum \mathrm{XY}=886$.
It was found later that the pair $(X=10, Y=5)$ was copied wrongly, instead of the correct value $(X=11, Y=4)$. Find the corrected value of correlation coefficient.

12a.i. What is probability mass function. (2marks)
ii A random variable X has the following probability distribution: (6marks)

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| $\mathrm{P}(\mathrm{x})$ | a | 3 a | 5 a | 7 a | 9 a | 11 a | 13 a | 15 a | 17 a |

(a) Determine the value of a. (b) Find $\mathrm{P}(2<\mathrm{X}<7)$
(c) What is the smallest value of x for which $\mathrm{P}(\mathrm{X} \leq \mathrm{x})>0.5$

12b. i. Prove that $\mathrm{P}(\mathrm{A} U \mathrm{~B})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})-\mathrm{P}(\mathrm{A} \cap \mathrm{B})$. (3marks)
ii A continuous random variable $X$ follows the probability law $f(x)=A x^{2} \quad 0 \leq x \leq 1$
Determine $\mathrm{A}, \mathrm{P}(0.2 \leq \mathrm{x} \leq 0.5)$ and $\mathrm{P}(\mathrm{x}>0.75)$ (5 marks)
13a .i. Define Normal distribution and state its properties.(3marks)
ii The mean weight of 600 students in a school is 50 kg ., and standard deviation is 6 kg . Assuming that the weights are normally distributed, find how many students weigh (a) between 44.5 kg . and 54.4 k . (b) less than 42.5 kg . ( 5 marks)
(or)
13b. i. Define Binomial distribution.
ii. The incident of certain disease is such that on an average $20 \%$ workers suffer from it. If 10 workers are selected at random, find the probability that exactly 2 workers suffer from the disease
and not more than 2 workers suffer from the disease.

14a. In the past, a chemical blending process has produced 15 kgs . or less of waste material for every 40 kgs . batch with a corresponding standard deviation of 5 kgs . From a sample of 25 batches, the accounting department now finds an average of 16 kgs . of waste/batch. At $5 \%$ level of significance, does the accounting department has reasons to believe that the average quantity of waste/batch has increased. (Z @ 5\% level = 1.64).

14b. Write the procedure for testing 400 times, which turns up head 219 times. Do the data justify the hypothesis of an unbiased coin? $\left(\mathrm{Z}_{0.025}=1.96\right)$. ( 8 marks )

15a. i. Define time series. (3marks)
ii the table below shows the production (metric ton) for a state for the year period 2000-2010 Construct (a) a 5-year moving average and (b) a 4-year moving average. (5marks)

| Year | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Production | 68 | 62 | 61 | 63 | 65 | 68 | 63 | 67 | 66 | 64 |

[^0]15bi. Explain semiaverages method. (3marks)
ii. Using the method of semiaverages, obtain the trend values for the purchase data (in thousands) given in the following table: (5marks)

| Year | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Purchase | 17.6 | 18.4 | 18.2 | 19.3 | 20.5 | 19.9 | 22.1 | 23.8 | 22.1 | 22.7 |

## PART C

## Answer any TWO Questions

16a. Find the Quartile deviation and Quotient of Quartile deviation for the following frequency distribution

| Wages/day(Rs.) | $150-159$ | $160-169$ | $170-179$ | $180-189$ | $190-199$ | $200-209$ | $210-219$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| No. of workers | 15 | 40 | 50 | 60 | 45 | 40 | 15 |

16b. A doctor has to visit a patient. From past experience it is known that probability with which he will come by train, bus, bike and by other means of transport are respectively $3 / 10$, $2 / 10,1 / 10$ and $4 / 10$. If he comes by train the probability that he will be late is $1 / 4$, by bus it is $1 / 3$, by bike it is $1 / 12$ and by other means of transport it is $1 / 3$. When he arrived, he was late. What is the probability that he came by train and by bike?

17a.i. Define the following: (a) random experiment (b) conditional probability. (5marks)
ii A group consisting of 15 men and 5 women from which a committee of 5 members is formed. What is the probability that the committee has
(a) 3 men, 2 women
(b) at least 2 men.
(5marks)
17b. i. Four coins are tossed simultaneously. What is the probability of getting
(a) no head
(b) two heads only.
(5marks)
ii The mean weight of 600 students in a school is 50 kg ., and standard deviation is 6 kg .
Assuming that the weights are normally distributed, find how many students weigh less than 42.5 kg .
(5 marks)

18a. Two sample poles of votes for two candidates A and B for a Public Office are taken, by choosing one from among residents of rural and urban areas. The results are given below. Examine whether the nature of the area is related to voting preference in this election.

| Vote for $\rightarrow$ <br> Area $\downarrow$ | A | B | Total |
| :--- | :--- | :--- | :--- |
| Rural | 620 | 380 | 1000 |
| Urban | 550 | 450 | 1000 |
| Total | 1170 | 830 | 2000 |

18b. . The lifetimes in hours of samples from three different types of T.V. picture tubes produced by a company is given below. Determine whether there is a difference between the three types at $5 \%$ level of significance. $F(2,9)=4.26$.

| Sample-1 | 407 | 411 | 409 | - | - |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Sample-2 | 404 | 406 | 408 | 405 | 402 |
| Sample-3 | 410 | 408 | 406 | 408 | - |

[^1]
[^0]:    (or)

[^1]:    Carry out the analysis of variance. (10marks)

